## Glass ball

The first photo here is taken with a digital camera and shows a glass ball, backlit with diffuse dichromatic light which has only two narrow spectral lines (red 630 nm and violet 400 nm ). This diffuse light comes from the white floor (marked with ' 1 ' in the figure) and the white walls (marked with ' 2 '), both illuminated with violet and red LED lamps. The sensor of the camera has only red, blue and green sensors so that violet light appears in the photo as blue. The photo is taken from a distance much greater than the radius of the ball. On the back side of the ball, a very narrow opaque thread is glued to the glass surface, forming an arc of a great circle on the ball. In the photo, the thread is obstructed by the ball and cannot be seen directly. However, hugely deformed images of a very short segment of the thread are seen as blue (marked
 with 'b') and red ('r') ellipses. The letter 'p' indicates purple-coloured areas in the photo.

In the first photo, the centre of the ball is marked with a cross, and the perimeter of the ball is traced with a dashed line. You can find a larger version of the first photo on a separate sheet. You may take distance measurements there. In the larger photo, the boundary between the red and purple regions is also traced with a dashed line.

The second photo is taken while illuminating with a white LED with the ball turned so that the thread can be seen directly.
a) Explain qualitatively using a ray diagram why a segment of the thread is seen as a closed loop in the first photo.
b) Determine the coefficient of refraction $n_{R}$ for the red light.
c) Determine the difference of the coefficients of refraction $\Delta n \equiv n_{V}-n_{R}$ for the red and violet light (with $n_{V}$ denoting the coefficient of refraction for the violet light)



